Abstract—Raptor codes are a class of Fountain codes that can reach data transmission rates at the capacity of the Binary Erasure Channels (BEC’s) and has, therefore, been extensively researched and refined for hard-decoding over these channels. These Raptor codes are ideal for packet transmission over the internet as they are a real world realization of the BEC’s. This article extends the Raptor codes for soft-decoding, investigates its performance over Additive White Gaussian Noise (AWGN) channels, which can potentially be used for wireless broadcast with asynchronous data access. We start by reviewing the conventional problem formalization for Fountain codes and consider the constraints common for both hard- and soft-decoding. We explain how the traditional belief propagation (BP) update rules may be transformed in order to avoid computation over large distributions. The loopy BP algorithm (a.k.a. sum-product algorithm) as well as 2 improvements, i.e. expectation propagation and inactivation decoding, are applied for soft-decoding in order to maximise the usage of the information available at the decoder. Simulation results over the AWGN channel of the decoding methods are compared.

I. INTRODUCTION

The pursuit for data transmission at rates close to the channel capacity has long been sought and, until recently, has merely been considered as theoretically feasible [1]. Then, in May 1993, a revolution occurred in coding theory with the release of a paper [2] that, almost by accident, combined sparse-graph codes with low-complexity iterative decoding thereby changing the way we approach error correcting codes. Today we have many codes, including turbo codes [2] and variations of low-density parity-check (LDPC) codes [3], [4] that perform close to channel capacity and may be implemented with low-complexity decoding algorithms. However, these codes have design difficulties due to their fixed code rates. Furthermore, they require that all packages be received and are received in order. These restrictions render these codes unsuitable for broadcasting [5].

Another class of codes, called fountain codes, does not suffer from these restrictions. The “digital fountain approach” concept was first introduced in [6] for communication over an erasure channel with unknown erasure probability. What makes fountain codes appropriate for broadcasting is that they are naturally rateless, i.e. for a given finite set of source packets, a fountain code can theoretically generate an infinite sequence of coded output packets. This is done while still retaining low complexity for both the encoding and decoding and therefore, remain viable codes for time constraint applications.

The first practical realization of a fountain code was the LT-code as introduced by M. Luby in [7] for Binary Erasure Channels (BEC). Initially, the LT-code divides the data file into equal packets, called source symbols, and encodes these into output symbols. Each of these output symbols is a linear combination of a random subset of the source symbols, as defined by an output degree distribution. These output symbols are then transmitted over the channel and decoded at the receiver to render the original source symbols. Due to the randomisation of the dependencies of the output symbol to the source symbols, the receiver may receive the output symbols in any order. Furthermore, as long as enough output symbols are received, we can successfully decode even when some output symbols are lost completely. This is ideal for broadcasting as explained in [5]. Unfortunately it turns out that, for reliable decoding, the length of the LT-code increases greatly with smaller increases of the code’s block length.

In this paper we will focus on an extension of the LT-code called the Raptor (rapid-tornado) code. Raptor codes first encode the initial source symbols with a sparse-graph code (usually LDPC codes), which we refer to as the pre-code, and thereafter continues to encode these new symbols (which we will refer to as input symbols) with the LT-code. This solves the problem of super-linear growth and yields linear time encoders and decoders [8]. This article also extends the Raptor codes for soft-decoding, which can potentially be used for wireless broadcast with asynchronous data access.

II. RAPTOR CODES

A. Graph structure of Raptor codes

The factor graph of an example Raptor code is presented in Fig. 1 and consists of 2 parts. The first, uppermost part of the graph is the pre-code with the input symbol gained after the initial source symbols were encoded with this pre-code. The pre-code factors define their XOR relationship to each other. In the lower part of the graph we have the LT-code to encode the output symbols as defined by the LT-factors, which define each output symbols’ XOR relationship to the input symbols. This graph structure applies to the transmitter and receiver alike, although at the receiver only the output symbols are received and the original input symbols are inferred from them, using this graph and some approximate inference algorithm.

B. Information transition over factors

We can define the decoding problem, from a probabilistic graphical model point of view, as the distribution of collected information over the factor graph. Initially the input symbol are undetermined at the receiver before decoding and each output symbol contains some information of the rest of the graph. Once we have collected enough output symbols we
will have enough information to determine the correct values of the input symbols, with high certainty.

However, having enough information in the global sense is not the only necessity for successful inference. We also require enough localised information to successfully transfer the information in the output symbols to the input symbols. Specifically, we need enough information over each factor in order to perform inference over it.

Take, for example, the LT-factor $f_0$ in Fig. 1. The relationship between its connected symbols is

$$y_0 \oplus z_0 \oplus z_1 = 0$$

where the modulo-2 addition (XOR) is represented by the symbol $\oplus$. Now let us assume that we know $y_0 = 1$ and nothing of $z_0$ and $z_1$. The previous equation then simplifies to

$$z_0 \oplus z_1 = 1$$

This still leaves us with 2 possible solutions. Thus, knowing only one symbol is not enough information to obtain a unique solution. In fact, for a factor of $N$ dependent symbols, we need to know the value of $N - 1$ symbols to obtain a unique solution.

This problem is true for soft-decision inference as well. In fact, the probability of the symbol we wish to compute will be more or less equal to the symbol with the lowest probability. Moreover, if 1 of the other symbols other than the one being computed has a probability distribution of $\{0.5, 0.5\}$, the resulting distribution will be the same. It is left for the reader to prove that this is true.

We therefore require a very specific graph structure in order to successfully propagate the information in each output symbol across the entire graph. For larger codes we may construct such a code by using an output degree distribution.

C. Degree distributions for fountain codes

As was just shown, to ensure a high probability of successful decoding, we need the output symbols’ dependencies to obtain such a structure that it ensures successful inference over all LT-factors. Although the output symbols’ dependencies are randomised, we can try to choose the input degree of these LT-factors in such a way that no redundancy exists in the structure of the graph, while ensuring proper inference. We would like to be able to transfer information to at least 1 new input symbol that does not yet contain any information at every iteration. For the theoretical Raptor code with endless output symbols, this can be achieved by the ideal soliton distribution [7], [10] defined as follows

$$\rho(d) = \begin{cases} \frac{1}{N} & \text{for } d = 1 \\ \frac{S}{N(d-1)} & \text{for } d = 2, 3, \ldots, N \end{cases}$$

where $d$ is the input degree of the LT-factor and $N$ is the total number of input symbols.

In practice, however, we will always have only a finite number of output symbols and in this case the ideal soliton distribution performs poorly. In [7] some adjustments were made to improve the distribution’s performance in practice. The result is called the Robust soliton distribution and is defined as follows

$$\tau(d) = \begin{cases} \frac{S}{dN} & \text{for } d = 1, 2, \ldots, (\frac{N}{S} - 1) \\ \frac{S}{N} \ln(\frac{S}{N}) & \text{for } d = \frac{N}{S} \\ 0 & \text{otherwise} \end{cases}$$

where $S \equiv c \ln(\frac{N}{S}) \sqrt{N}$ for some suitable choice of $c$ and $\delta$. For more on how to choose these parameters the reader is referred to [7].

D. Encoding of Raptor codes

Let us assume a data file of length $L$ which we wish to transmit. To minimise packet overhead we choose the symbol size $l$ and divide the data file into $D = \frac{L}{l}$ symbols. These symbols are then encoded using some sparse code such as LDPC codes (in Fig. 1 we used the Hamming (7,4) code).

We then generate the output symbols on-the-fly according to the following steps:

1) Choose the degree $d$ of the new output symbol randomly from a degree distribution such as the Robust soliton distribution.
2) Choose uniformly $d$ different random input symbols as dependencies of the new symbol.
3) The output symbol will be the result of the XOR on the $d$ chosen input symbols to satisfy even parity.

Output symbols are produced until decoding is successful.

III. BELIEF PROPAGATION

The decoding of Raptor codes are most often done using the Believe-Propagation (BP) algorithm (a.k.a the sum-product algorithm). In the following section we explain how the traditional BP update rules can be transformed in order to avoid computation over large distributions and how they are used to decode the Raptor code.

A. Conversion of update rules

The BP algorithm uses message-passing over bipartite Tanner graphs [11] (such as the one in Fig. 1) to decode a transmitted code word. More specifically, these graphs consist of 2 disjointed sets; variable nodes and factor nodes. A message passed along the edge between an arbitrary symbol $x_n$ (which may be any input or output symbol) and factor $f_m$ is one of the two following possible update rules, as defined in [9], [12]:

$$\begin{align*}
\text{if } f_m \text{ is an input symbol: } & x_n \leftarrow x_n \oplus f_m \\
\text{if } f_m \text{ is an output symbol: } & f_m \leftarrow f_m \oplus x_n
\end{align*}$$
Considering that Raptor codes consist of discrete variables, the number of entries in the distribution of $f_m(x_m)$ is exponential to the number of symbols in $x_m$ i.e. $2^{|x_m|}$. For sparse graphs such as those of LDPC codes, the factors remain small and thus these equations suffice for low complexity and reliable inference. However, due to the Robust soliton distribution introduced in Section II we are almost guaranteed to have factors of high density. These dense factors greatly increases the complexity of decoding and computations done over their distributions become intractable to the extent that decoding is NP-hard.

Fortunately we can avoid computation over these large distribution tables by making the observation that our factors enforce even parity over their dependencies. This allows us to re-express the BP algorithm for the special case of even parity, using the Log Likelihood Ratio (LLR) form [12], [13].

Firstly we would like to define a function to describe the even parity constraint. We know that even parity is the equivalent of the modulo-2 addition (XOR). For the case of an 2 independent Binary Random Variables (BRVs) $x$ and $y$, with probability distributions $P(x) = \{p_0^x, p_1^x\}$ and $P(y) = \{p_0^y, p_1^y\}$, the probability for even parity is:

$$P(x \oplus y = 0) = p_0^x p_0^y + p_1^x p_1^y$$

$$= (p_0^x + p_1^x)(p_0^y + p_1^y) - (p_0^x p_0^y + p_1^x p_1^y)$$

$$= \frac{1}{2}((p_0^x + p_1^x)(p_0^y + p_1^y) + (p_0^x - p_1^x)(p_0^y - p_1^y))$$

By induction we can extend this for an arbitrary finite amount of BRV’s $x_i$ for $i = 0, 1, 2, \ldots, N$. Then we have:

$$P\left(\sum_{i=0}^{N} x_i = 0\right) = \frac{1}{2}\left(\prod_{i=0}^{N} (p_0^{(i)} + p_1^{(i)}) + \prod_{i=0}^{N} (p_0^{(i)} - p_1^{(i)})\right)$$

$$P\left(\sum_{i=0}^{N} x_i = 1\right) = \frac{1}{2}\left(\prod_{i=0}^{N} (p_0^{(i)} + p_1^{(i)}) - \prod_{i=0}^{N} (p_0^{(i)} - p_1^{(i)})\right)$$

Notice that the term $\prod_{i=0}^{N} (p_0^{(i)} + p_1^{(i)}) = 1$, however we will not implement this simplification as this will not be the case once we convert these equations to the LLR domain.

We will define the LLR of the BRV $x$ as $L(x) = \ln\left(\frac{P(x=0)}{P(x=1)}\right)$. This also implies the following relationships:

$$P(x = 0) = \frac{e^{L(x)}}{1 + e^{L(x)}}$$

$$P(x = 1) = \frac{1}{1 + e^{L(x)}}$$

Furthermore, considering that the incoming message in equation (2) are of independent symbols in LLR form, it is useful to use the symbol $\oplus$ as the notation for the addition defined as:

$$L(x_1) \oplus L(x_2) \oplus \ldots \oplus L(x_N) \equiv L(x_1 \oplus x_2 \oplus \ldots \oplus x_N)$$

To retain mathematical integrity the following additional rules also apply [13]:

$$L(x) \oplus \infty = L(x)$$

$$L(x) \oplus -\infty = -L(x)$$

$$L(x) \oplus 0 = 0$$

Using equations (3) to (6) we can extend equation (7) such that

$$\sum_{i=0}^{N} L(x_i) \equiv L\left(\sum_{i=0}^{N} x_i\right)$$

$$= \ln\left(\prod_{i=0}^{N} \left(e^{L(x_i)} + 1\right) + \prod_{i=0}^{N} \left(e^{L(x_i)} - 1\right)\right)$$

$$\prod_{i=0}^{N} \left(e^{L(x_i)} + 1\right) - \prod_{i=0}^{N} \left(e^{L(x_i)} - 1\right)$$

Using the identity $\tanh\left(\frac{x}{2}\right) = \frac{e^x - 1}{e^x + 1}$ we can simplify

$$\sum_{i=0}^{N} L(x_i) \equiv \ln\left(\frac{1 + \prod_{i=0}^{N} \tanh\left(\frac{L(x_i)}{2}\right)}{1 - \prod_{i=0}^{N} \tanh\left(\frac{L(x_i)}{2}\right)}\right)$$

furthermore, if we define $\kappa = 1 + \prod_{i=0}^{N} \tanh\left(\frac{L(x_i)}{2}\right)$ then

$$\tanh\left(\frac{1}{2} \sum_{i=0}^{N} L(x_i)\right) = \ln\left(\frac{1 + \kappa}{1 - \kappa}\right) - 1$$

$$= \ln\left(\frac{1 + \kappa}{1 - \kappa}\right) + 1$$

$$= (1 + \kappa) + (1 - \kappa)$$

$$= \kappa$$

Therefore we conclude that

$$\sum_{i=0}^{N} L(x_i) \equiv 2 \tanh^{-1}\left(\prod_{i=0}^{N} \tanh\left(\frac{L(x_i)}{2}\right)\right)$$

Let us now consider the BP updating rules (1) and (2). To help distinguish between the linear and LLR domains we will define the following relationship

$$\lambda_{x_n \rightarrow f_m}(x_n) \equiv L(\mu_{x_n \rightarrow f_m}(x_n))$$

$$\lambda_{f_m \rightarrow x_n}(x_n) \equiv L(\mu_{f_m \rightarrow x_n}(x_n))$$

It is thus easy to show that the updating rule for variable to factor message (1) now becomes:

$$L(\mu_{x_n \rightarrow f_m}(x_n)) = L\left(\prod_{f_i \in f_m, f_i \neq x_n} \mu_{f_i \rightarrow x_n}(x_n)\right)$$

$$\lambda_{x_n \rightarrow f_m}(x_n) = \sum_{f_i \in f_m, f_i \neq x_n} \lambda_{f_i \rightarrow x_n}(x_n)$$

The LLR transformation of the updating rule for factor to variable is somewhat more elaborate. As mentioned before,
Fig. 2. A sub-graph of an arbitrary factor graph, showing a symbol $x$, factor $f$ and the two types of messages sent along the edges of a graph that are involved in the BP algorithm. $x$ will only transmit $\mu_{x \rightarrow f}(x)$ once it has received a message from all other factors it shares an edge with. Similarly, factor $f$ will not transmit $\mu_{f \rightarrow x}(x)$ before it has received all messages from all the symbols it is connected to.

$f_{m}(x_{m})$ enforces even parity and thus the summation over this distribution can be represented as a modulo-2 addition, such that

$$\sum_{x_{m}\setminus x_{n}} f_{m}(x_{m}) \prod_{x_{i} \in x_{m}\setminus x_{n}} P(x_{i}) \equiv P \left( \prod_{x_{i} \in x_{m}\setminus x_{n}} \mu_{x_{i} \rightarrow f}(x_{i}) \right)$$

With this knowledge we may continue our transformation of the updating rule for factor to variable messages (2):

$$L(\mu_{f \rightarrow x_{n}}(x_{n})) = L \left( \sum_{x_{m}\setminus x_{n}} f_{m}(x_{m}) \prod_{x_{i} \in x_{m}\setminus x_{n}} \mu_{x_{i} \rightarrow f}(x_{i}) \right)$$

$$\lambda_{f \rightarrow x_{n}}(x_{n}) = L \left( \sum \prod_{x_{i} \in x_{m}\setminus x_{n}} \mu_{x_{i} \rightarrow f}(x_{i}) \right) = \sum \lambda_{x_{i} \rightarrow f}(x_{i})$$

which leaves us with the new updating rule

$$\lambda_{f \rightarrow x_{n}}(x_{n}) = 2 \tanh^{-1} \left( \prod_{i=0}^{N} \tanh \left( \frac{\lambda_{x_{i} \rightarrow f}(x_{i})}{2} \right) \right) \tag{9}$$

B. Message passing

The BP algorithm was originally designed for tree-like Tanner graphs and, unfortunately, Raptor codes in general contain many loops. However, these loops are generally large enough that the code is tree-like over the span of localised sub-graphs which allows us to use the LBP algorithm.

LBP is an iterative process where the messages (equations (8) and (9)) are passed across the graph until convergence. This algorithm will not produce exact inference as in the case of tree-like graphs, nor does it guarantee convergence. However, despite these shortfalls it has been proved to achieve good decoding performance and thus remains useful in practice [14].

The message passing schedule applied in this paper is called message flooding. We start by initiating all messages from variables symbols to become

$$\lambda_{x_{n} \rightarrow f}(x_{n}) = 0$$

which is often referred to as lazy initialization. This causes all factor nodes to receive a message across all of their edges, enabling them to transmit a new message back to those same variable symbols in turn. If Fig. 2 is considered, the message $\lambda_{x \rightarrow f}(x)$ will initially be 0. The factor $f$ receives this message and all other messages across all other edges connected to that. It then updates its messages using equation (9) and returns message $\lambda_{f \rightarrow x}(x)$ and all other messages across all other edges. Symbol $x$ goes through a similar process using equation (8). This process continues until convergence occurs.

IV. IMPROVEMENTS ON BELIEF PROPAGATION

A. Tree-structure Expectation propagation

As mentioned before, one fundamental problem with fountain codes is that enough input degree 1 ($N = 1$) LT-factors are required in order to initiate the BP algorithm. Conventionally this problem is overcome by introducing very large fountain codes. However with very little or no increase in complexity we can use the relationship of the input and output symbols, as defined by the LT-factors, to change the structure of the factor graph in order to obtain the necessary $N = 1$ LT-factors.

An algorithm called Tree-structure Expectation Propagation (TEP) is proposed and analysed in [15]. It changes the graph structure to decode LDPC codes over the Binary Erasure Channel (BEC). In [16] (this algorithm was analysed for the LT-code over the BEC. Here we will adapt the algorithm for Raptor/LT code over the Additive White Gaussian Noise (AWGN) channels (i.e. soft-decoding).

TEP is only triggered once the BP fails as described in Section II-B. The algorithm starts by searching for the first $N = 2$ LT-factor ($f_{0}$) that is a function of the two input symbols ($z_{0}$ and $z_{1}$) as depicted in Fig. 3. Once found, this factor is added to a list which will exclude it from searches in future iterations of the algorithm. Thereafter, one of the two input symbols is chosen ($z_{1}$). All LT-factors, other than the originally chosen factor ($f_{0}$), that shares an edge with both $z_{0}$ and $z_{1}$ have both edges removed. Each LT-factor sharing an edge with $z_{1}$, but not with $z_{0}$, has its link to $z_{1}$ removed and a link to $z_{0}$ added. Furthermore, all output symbols connected to $f_{0}$ ($y_{0}$) are connected to each factor that had its links to $z_{1}$ and/or $z_{0}$ removed. Finally, once the graph restructuring is done, the algorithm will try to implement BP again and if decoding is not successful the process will be repeated.

In the example of Fig. 3 the TEP algorithm is successful in producing a $N = 1$ factor ($f_{2}$). In fact the TEP algorithm will only be successful if and only if a $N = 3$ LT-factor share both the input symbols of the chosen $N = 2$ LT-factor with it. However, it is shown in [15] that the probability of producing a $N = 1$ factor increases exponentially after each iteration of the algorithm.

The TEP algorithm is based upon a basic observation that the relationship as defined by the LT-factor can be viewed as simultaneous XOR equations. Thus, for the instance in Fig. 3a we have,

$$y_{0} = z_{0} \oplus z_{1} \quad y_{2} = z_{0} \oplus z_{1} \oplus z_{2}$$

$$y_{1} = z_{1} \oplus \ldots \quad y_{3} = z_{0} \oplus \ldots$$

The order of the variables does not matter, thus we may also write the first equation as $y_{1} = y_{0} \oplus z_{0}$. We can now substitute this into the other equation to remove $z_{1}$, leaving us with

$$y_{0} = z_{0} \oplus z_{1} \quad y_{0} \oplus y_{2} = z_{0} \oplus z_{0} \oplus z_{2}$$

$$y_{0} \oplus y_{1} = z_{0} \oplus \ldots \quad y_{3} = z_{0} \oplus \ldots$$
Note that a variable XOR’ed with itself is 0, therefore the third equation reduces to $y_0 \oplus y_2 = z_2$. These final equations now represent the relationships in Fig. 3b.

### B. Inactivation decoding

The following algorithm, termed Inactivation decoding (ID), was developed in order to combine the decoding success rate of Gaussian elimination with the low complexity of belief propagation [17] and is analysed for BEC’s in [5]. Once again we will make minor adaptations to the algorithm for soft decoding over AWGN channels.

Before the algorithm starts, all input symbols are considered active symbols. Only active symbols are included when calculating $\mathcal{N}$ of a LT-factor. The algorithm starts by searching for a LT-factor of $\mathcal{N} = 1$. Once found it performs Gaussian elimination on the LT-constraint matrix (or equivalent operations on the factor graph), thus eliminating the active input symbol from all other LT-factors. Just as with TEP, we add a link between all output symbols connected to the $\mathcal{N} = 1$ LT-factor and those which had the variable removed. The corresponding input symbol of the $\mathcal{N} = 1$ LT-factor is now considered recovered and is excluded from the rest of the algorithm until BP is applied to the final factor graph. A simple example is depicted in Fig. 4, where input symbol $z_5$ is to be recovered via LT-factor $f_3$. ID replaces the edges $z_5$ to $f_4$ and $z_5$ to $f_6$ with the edges $y_5$ to $f_4$ and $y_5$ to $f_6$, respectively.

This process continues until no $\mathcal{N} = 1$ exists. If this is the case, the algorithm inactivates an input symbol that has not yet been recovered. By doing so the inactivated symbol will be ignored when choosing a factor to eliminate, i.e. all factors connected to the inactivated symbol have their input degree reduced by one. After a symbol has been inactivated, the algorithm once again searches for a LT-factor of $\mathcal{N} = 1$. If none is found another input symbol is inactivated. This continues until all input variables are either recovered or inactivated. This adds another constraint to the ID: there needs to be at least as many LT-factors (thus output symbols) as there are input symbols. Finally, BP is applied to the new factor graph.

In many ways this algorithm is very similar to TEP, in fact the instance depicted in Fig. 3 can be viewed as a special case of recovery of $z_1$, where $z_0$ is inactivated. However ID manipulates the graph structure to a greater extent and does not wait for BP to fail before initiating. Therefore both these algorithms end up with vastly different factor graphs and, as we shall see, vastly different decoding performances.

### V. PERFORMANCE EVALUATION

#### A. Simulation parameters

For testing transmission over the binary AWGN channel, we used binary inputs $\{-1, +1\}$ to represent input bit values $\{0, 1\}$ respectively. We tested the 3 decoding algorithms described in this paper on a Raptor code with the precode of the R10 code (a standard code used in the industry [5]). A small block size of $B = 50$ bits was used to reduce simulation time. Although these small codes do not fare as well as larger codes, they suffice to depict the behaviour of the 3 algorithms. The symbol size over all simulations was set to 1 bit as we assumed synchronous communication between sender and receiver, thereby negating the necessity for package headers. Subsequently the same performance will be obtained for larger symbol sizes.

Simulations were run to compare the rate of block decoding failure (block error rate) against the noise variances $\sigma$. $\sigma$ is incremented in steps of 0.05 from 0 to 1, and each data point is the result over 500 iterations. The overhead was chosen as $30\%$ and $100\%$, where the overhead is measured as the percentage of output symbols compared to the input symbols. Unfortunately, the differences between hard- and soft-decoding are of such a nature that comparing them is nonsensical, thus we do not compare our simulation result over AWGNC to that of conventional BEC.
in order to avoid computation over large distributions. We continued to apply and simulate the loopy BP, EP and ID algorithms on a Raptor code for soft-decoding and compared the results.

It is clear that, although ID has a good performance at low overhead, it is outperformed by BP and TEP at higher overhead levels. In contrast, BP and TEP has a poorer performance at low noise levels, but has a greater resistance against increasing noise levels if a large overhead is provided.

Future work include investigating the junction tree algorithm to avoid loopy inference and the necessity for $N = 1$ LT-factors. This may be combined with techniques to approximate the very large clusters of junction trees. Furthermore, damping techniques might be used on the messages in order to reduce the oscillations of message values to in effect, improve message convergence and thus decoding performance.

**References**


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